# Towards Diverse and Coherent Augmentation for Time-Series Forecasting

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- Motivation
- Method
- Experiments
- Conclusion

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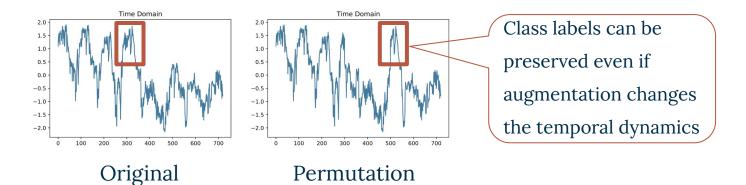
- Data scarcity in time series is very common
  - Malfunctioning sensors due to battery depletion
  - Privacy concerns in medical domain
  - $\circ$   $\,$  Cold-start prediction for new stations or new stores



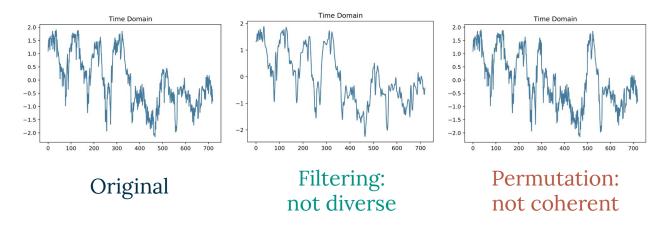




- Data augmentation mitigates the data scarcity issue
- Existing time-series augmentation methods are mainly designed for classification



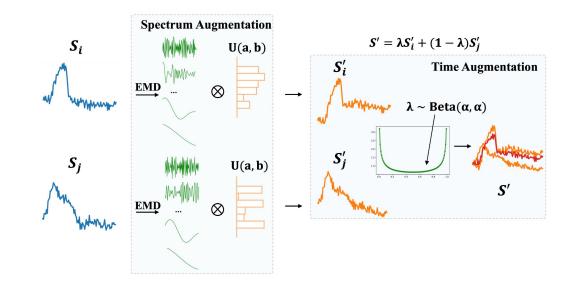
• Augmentation for time-series forecasting requires diversity as well as coherence with the temporal dynamics



- Unlike images or text, time-series data generated by real-life physical processes have characteristics in both time and spectral domains
- Our contribution: Combining **S**pectral and **T**ime **Aug**mentation (**STAug**) to generate more diverse and coherent samples for time-series forecasting

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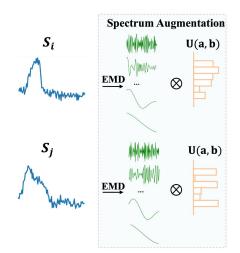
• Combine frequency-domain augmentation and time-domain augmentation



• Frequency-domain augmentation: decompose time series with Empirical Mode Decomposition (EMD), and reassemble subcomponents with random weights

$$\mathbf{S} = \sum_{i=1}^{n} \mathrm{IMF}_{i} + \mathbf{R} \qquad \mathbf{S}' = \sum_{i=1}^{n} w_{i} \cdot \mathrm{IMF}_{i}$$

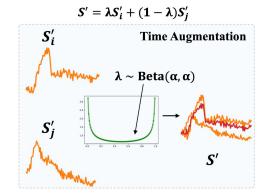
- Diversity: random weights to combine components
- Coherence: augmented samples have the same set of base components



• Time-domain augmentation: mix up values at both history and future time steps

$$\mathbf{H}' = \lambda \mathbf{H}_{\mathbf{i}} + (1 - \lambda) \mathbf{H}_{\mathbf{j}} \qquad \mathbf{F}' = \lambda \mathbf{F}_{\mathbf{i}} + (1 - \lambda) \mathbf{F}_{\mathbf{j}}$$

- Diversity: random weights to combine series pairs
- Coherence: only generate linearly in-between samples by the interpolation nature of "mix up"



- During training, we apply both frequency-domain and time-domain augmentation to obtain an augmented sample
- Optimize the downstream forecasting model with augmented samples as input

$$\mathcal{L} = rac{1}{N} \sum_{i=1}^{N} ||\mathbf{Y_i} - \mathbf{F'_i}||_2^2$$

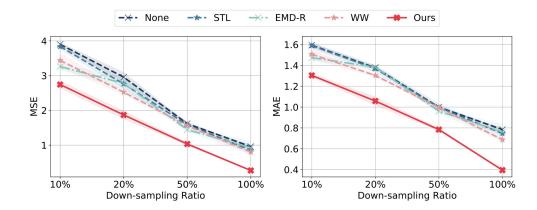
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- Experiments
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- Datasets: ETTh1, ETTh2, ETTm1, ETTm2, Exchange
- Forecasting backbone model: Informer (AAAI' 21 best paper)
- Baselines: basic random operations (WW, RobustTAD), decomposition-based augmentation (STL, EMD-R), pattern mixing method (DBA), generative method (GAN)

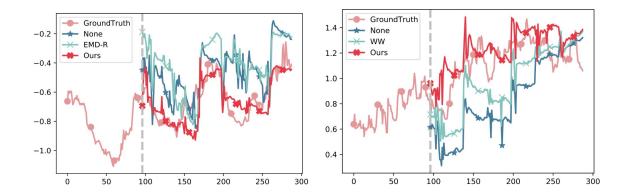
• STAug reduces average MSE by 28.2% and average MAE by 18.0% compared with the best baseline for each of the five datasets

Methods		None		ww		RobustTAD		STL		EMD-R		GAN		DBA		STAug-noTime		STAug-noFreq		STAug	
Metric		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTh1	96 192 336 720	$\begin{array}{c} 0.95{\pm}0.06\\ 0.98{\pm}0.02\\ 1.11{\pm}0.04\\ 1.18{\pm}0.03\end{array}$	$\substack{0.76 \pm 0.04 \\ 0.77 \pm 0.02 \\ 0.83 \pm 0.02 \\ 0.86 \pm 0.02 }$	$0.89 \pm 0.06$ $1.00 \pm 0.12$ $1.06 \pm 0.03$ $1.20 \pm 0.02$	$\substack{0.73 \pm 0.04 \\ 0.78 \pm 0.08 \\ 0.81 \pm 0.02 \\ 0.88 \pm 0.01 }$	$\substack{1.01\pm0.03\\0.95\pm0.02\\1.09\pm0.06\\1.15\pm0.02}$	$\substack{0.79 \pm 0.01 \\ 0.74 \pm 0.01 \\ 0.82 \pm 0.04 \\ 0.84 \pm 0.01 }$	$\substack{0.91\pm0.05\\0.94\pm0.02\\1.09\pm0.04\\1.19\pm0.02}$	$\begin{array}{c} 0.74{\pm}0.03\\ 0.74{\pm}0.02\\ 0.81{\pm}0.02\\ 0.86{\pm}0.01\end{array}$	$\begin{array}{c} 0.84{\pm}0.05\\ 0.94{\pm}0.04\\ 1.06{\pm}0.02\\ 1.19{\pm}0.02\end{array}$	$\begin{array}{c} 0.69{\pm}0.03\\ 0.73{\pm}0.04\\ 0.80{\pm}0.01\\ 0.87{\pm}0.01 \end{array}$	$0.90 \pm 0.08$ $0.99 \pm 0.04$ $1.07 \pm 0.01$ $1.22 \pm 0.04$	$\substack{0.73 \pm 0.06 \\ 0.76 \pm 0.03 \\ 0.82 \pm 0.01 \\ 0.89 \pm 0.01 }$	$\substack{0.94 \pm 0.06 \\ 0.98 \pm 0.02 \\ 1.11 \pm 0.04 \\ 1.18 \pm 0.03 }$	$\begin{array}{c} 0.76 {\pm} 0.04 \\ 0.77 {\pm} 0.02 \\ 0.83 {\pm} 0.02 \\ 0.87 {\pm} 0.02 \end{array}$	$\begin{array}{c} 0.66 {\pm} 0.01 \\ \hline \textbf{0.75 {\pm} 0.02} \\ \textbf{0.86 {\pm} 0.02} \\ \hline 0.99 {\pm} 0.06 \end{array}$	$\begin{array}{c} \underline{0.57 \pm 0.01} \\ \hline \textbf{0.62 \pm 0.01} \\ \hline \textbf{0.68 \pm 0.01} \\ \underline{0.75 \pm 0.03} \end{array}$	$0.84 \pm 0.06$ $0.96 \pm 0.00$ $1.10 \pm 0.06$ $1.16 \pm 0.01$	$\substack{0.69 \pm 0.03 \\ 0.76 \pm 0.01 \\ 0.83 \pm 0.03 \\ 0.86 \pm 0.01 }$	$\begin{array}{c} \textbf{0.65 {\pm} \textbf{0.01}} \\ \underline{0.77 {\pm} 0.03} \\ \underline{0.89 {\pm} 0.02} \\ \textbf{0.97 {\pm} \textbf{0.00}} \end{array}$	$\begin{array}{c} \textbf{0.57}{\pm}\textbf{0.01} \\ \underline{0.63}{\pm}0.02 \\ \underline{0.71}{\pm}0.01 \\ \textbf{0.75}{\pm}\textbf{0.00} \end{array}$
ETTh2	96 192 336 720	$3.08 \pm 0.62$ $5.97 \pm 0.30$ $4.78 \pm 0.33$ $3.99 \pm 0.27$	$\substack{1.38 \pm 0.13 \\ 2.02 \pm 0.05 \\ 1.83 \pm 0.08 \\ 1.69 \pm 0.06}$	$3.40 \pm 0.48$ $6.43 \pm 0.68$ $4.97 \pm 0.07$ $3.83 \pm 0.13$	$\substack{1.46 \pm 0.11 \\ 2.10 \pm 0.09 \\ 1.85 \pm 0.05 \\ 1.68 \pm 0.04 }$	$3.03 \pm 0.25$ $6.20 \pm 0.35$ $5.29 \pm 0.15$ $3.90 \pm 0.13$	$1.38 \pm 0.05$ $2.08 \pm 0.05$ $1.88 \pm 0.01$ $1.66 \pm 0.00$	$3.04 \pm 0.48$ $5.89 \pm 0.46$ $4.77 \pm 0.24$ $3.56 \pm 0.04$	$\substack{1.37 \pm 0.11 \\ 2.02 \pm 0.08 \\ 1.83 \pm 0.05 \\ 1.58 \pm 0.03 }$	$\begin{array}{c} 3.44{\pm}0.29\\ 6.33{\pm}0.10\\ 5.44{\pm}0.18\\ 4.08{\pm}0.09\end{array}$	$\substack{1.45 \pm 0.05 \\ 2.09 \pm 0.00 \\ 1.95 \pm 0.05 \\ 1.72 \pm 0.03 }$	$\begin{array}{c} 2.91{\pm}0.36\\ 5.47{\pm}0.30\\ 4.91{\pm}0.31\\ 4.06{\pm}0.41\end{array}$	$\substack{1.38 \pm 0.09 \\ 1.94 \pm 0.05 \\ 1.87 \pm 0.06 \\ 1.74 \pm 0.10 }$	$3.01 \pm 0.54$ $5.64 \pm 0.47$ $4.77 \pm 0.32$ $4.01 \pm 0.27$	$\begin{array}{c} 1.37{\pm}0.12\\ \hline 1.94{\pm}0.09\\ \hline 1.83{\pm}0.08\\ \hline 1.70{\pm}0.06\end{array}$	$\begin{array}{c} \textbf{1.80 \pm 0.11} \\ \underline{4.02 \pm 0.23} \\ \underline{3.39 \pm 0.27} \\ \underline{2.70 \pm 0.30} \end{array}$	$\frac{1.01 \pm 0.04}{1.57 \pm 0.05}$ $\frac{1.48 \pm 0.07}{1.38 \pm 0.09}$	$\substack{2.98 \pm 0.57 \\ 5.23 \pm 0.15 \\ 4.37 \pm 0.26 \\ 3.57 \pm 0.18 }$	$\substack{1.37 \pm 0.14 \\ 1.89 \pm 0.03 \\ 1.74 \pm 0.05 \\ 1.62 \pm 0.04}$	$\begin{array}{r} \underline{1.87 \pm 0.30} \\ \overline{\textbf{3.47 \pm 0.24}} \\ \textbf{3.37 \pm 0.14} \\ \textbf{2.62 \pm 0.17} \end{array}$	$\frac{1.05\pm0.09}{\textbf{1.48}\pm\textbf{0.06}}\\\frac{1.51\pm0.04}{\textbf{1.34}\pm\textbf{0.08}}$
ETTm1	96 192 336 720	$\begin{array}{c} 0.63 {\pm} 0.03 \\ 0.80 {\pm} 0.04 \\ 1.15 {\pm} 0.07 \\ 1.13 {\pm} 0.04 \end{array}$	$\substack{0.57 \pm 0.01 \\ 0.67 \pm 0.02 \\ 0.84 \pm 0.03 \\ 0.81 \pm 0.00}$	$\substack{0.63 \pm 0.02 \\ 0.79 \pm 0.07 \\ 1.00 \pm 0.06 \\ 1.08 \pm 0.07 }$	$\substack{0.57 \pm 0.01 \\ 0.67 \pm 0.03 \\ 0.77 \pm 0.03 \\ 0.79 \pm 0.02 }$	$\substack{0.59 \pm 0.03 \\ 0.80 \pm 0.08 \\ 0.98 \pm 0.04 \\ 1.06 \pm 0.04 }$	$\substack{0.55 \pm 0.02 \\ 0.66 \pm 0.04 \\ 0.76 \pm 0.03 \\ 0.79 \pm 0.03 }$	$\substack{0.55 \pm 0.03 \\ 0.74 \pm 0.06 \\ 0.99 \pm 0.07 \\ 1.18 \pm 0.02 }$	$\substack{0.53 \pm 0.01 \\ 0.65 \pm 0.03 \\ 0.77 \pm 0.03 \\ 0.82 \pm 0.00 }$	$\begin{array}{c} 0.64{\pm}0.01\\ 0.68{\pm}0.01\\ 0.87{\pm}0.14\\ 1.01{\pm}0.10 \end{array}$	$\substack{0.56 \pm 0.00 \\ 0.59 \pm 0.01 \\ 0.70 \pm 0.06 \\ 0.75 \pm 0.05 }$	$\substack{0.63 \pm 0.02 \\ 0.84 \pm 0.06 \\ 0.90 \pm 0.07 \\ 1.23 \pm 0.12}$	$\substack{0.58 \pm 0.01 \\ 0.69 \pm 0.02 \\ 0.73 \pm 0.04 \\ 0.86 \pm 0.04 }$	$\substack{0.63 \pm 0.03 \\ 0.80 \pm 0.03 \\ 1.15 \pm 0.06 \\ 1.13 \pm 0.04 }$	$\begin{array}{c} 0.57{\pm}0.02\\ 0.68{\pm}0.02\\ 0.84{\pm}0.02\\ 0.81{\pm}0.01 \end{array}$	$\begin{array}{c} \underline{0.43 \pm 0.00} \\ \underline{0.54 \pm 0.02} \\ \underline{0.65 \pm 0.03} \\ \underline{0.83 \pm 0.03} \end{array}$	$\begin{array}{c} \underline{0.44 {\pm} 0.00} \\ \underline{0.51 {\pm} 0.00} \\ \underline{0.57 {\pm} 0.02} \\ \underline{0.66 {\pm} 0.01} \end{array}$	$\begin{array}{c} 0.55 {\pm} 0.03 \\ 0.67 {\pm} 0.04 \\ 0.90 {\pm} 0.02 \\ 0.93 {\pm} 0.10 \end{array}$	$\substack{0.53 \pm 0.02 \\ 0.59 \pm 0.02 \\ 0.72 \pm 0.01 \\ 0.72 \pm 0.04 }$	$\substack{ 0.40 \pm 0.00 \\ 0.49 \pm 0.00 \\ 0.63 \pm 0.03 \\ 0.76 \pm 0.04 }$	$\begin{array}{c} 0.42{\pm}0.00\\ 0.48{\pm}0.00\\ 0.56{\pm}0.01\\ 0.63{\pm}0.02 \end{array}$
ETTm2	96 192 336 720	0.42±0.06 0.78±0.09 1.52±0.07 3.46±0.27	$\substack{0.51 \pm 0.04 \\ 0.68 \pm 0.03 \\ 0.95 \pm 0.02 \\ 1.42 \pm 0.08 }$	$\substack{0.39 \pm 0.02 \\ 0.78 \pm 0.09 \\ 1.43 \pm 0.08 \\ 4.37 \pm 0.29 }$	$\substack{0.48 \pm 0.02 \\ 0.68 \pm 0.04 \\ 0.92 \pm 0.02 \\ 1.64 \pm 0.08 }$	$\begin{array}{c} 0.39 {\pm} 0.02 \\ 0.88 {\pm} 0.20 \\ 1.39 {\pm} 0.18 \\ 4.79 {\pm} 0.03 \end{array}$	$\begin{array}{c} 0.48 {\pm} 0.01 \\ 0.72 {\pm} 0.10 \\ 0.91 {\pm} 0.07 \\ 1.65 {\pm} 0.01 \end{array}$	$\substack{0.39 \pm 0.03 \\ 0.71 \pm 0.05 \\ 1.40 \pm 0.06 \\ 3.27 \pm 0.30 }$	$0.49 \pm 0.03$ $0.65 \pm 0.01$ $0.91 \pm 0.03$ $1.38 \pm 0.08$	$\begin{array}{c} 0.40{\pm}0.08\\ 0.54{\pm}0.04\\ 1.29{\pm}0.04\\ 3.25{\pm}0.35\end{array}$	$\begin{array}{c} 0.48{\pm}0.05\\ 0.55{\pm}0.03\\ 0.88{\pm}0.02\\ 1.35{\pm}0.07\end{array}$	$\substack{ 0.33 \pm 0.03 \\ 0.63 \pm 0.11 \\ 1.45 \pm 0.12 \\ 3.13 \pm 0.71 }$	$\begin{array}{c} 0.43 {\pm} 0.03 \\ 0.60 {\pm} 0.05 \\ 0.93 {\pm} 0.05 \\ 1.36 {\pm} 0.17 \end{array}$	$\substack{0.42 \pm 0.05 \\ 0.77 \pm 0.07 \\ 1.57 \pm 0.10 \\ 3.48 \pm 0.27 }$	$\begin{array}{c} 0.51{\pm}0.04\\ 0.67{\pm}0.03\\ 0.96{\pm}0.03\\ 1.43{\pm}0.08 \end{array}$	$\begin{array}{c} \underline{0.30 \pm 0.03} \\ \hline \textbf{0.42 \pm 0.00} \\ \underline{0.94 \pm 0.19} \\ \hline \textbf{2.65 \pm 0.47} \end{array}$	$\begin{array}{c} \underline{0.39 {\pm} 0.01} \\ \hline \textbf{0.49 {\pm} 0.01} \\ \underline{0.74 {\pm} 0.07} \\ \hline \textbf{1.20 {\pm} 0.10} \end{array}$	$\begin{array}{c} 0.33 {\pm} 0.06 \\ 0.59 {\pm} 0.01 \\ 1.29 {\pm} 0.11 \\ 3.77 {\pm} 0.38 \end{array}$	$\substack{0.42 \pm 0.04 \\ 0.59 \pm 0.01 \\ 0.88 \pm 0.03 \\ 1.51 \pm 0.10}$	$\begin{array}{c} \textbf{0.29}{\pm}\textbf{0.03} \\ \underline{0.43}{\pm}0.02 \\ \hline \textbf{0.81}{\pm}\textbf{0.03} \\ \underline{2.79}{\pm}0.25 \end{array}$	$\begin{array}{c} \textbf{0.39 \pm 0.03} \\ \underline{0.50 \pm 0.01} \\ \textbf{0.69 \pm 0.01} \\ \underline{1.27 \pm 0.04} \end{array}$
Exchange	96 192 336 720	$\begin{array}{c} 0.96{\pm}0.04\\ 1.11{\pm}0.01\\ 1.61{\pm}0.04\\ 2.85{\pm}0.16\end{array}$	$\begin{array}{c} 0.78 {\pm} 0.01 \\ 0.84 {\pm} 0.00 \\ 1.01 {\pm} 0.02 \\ 1.39 {\pm} 0.04 \end{array}$	$\begin{array}{c} 0.80 {\pm} 0.06 \\ 1.08 {\pm} 0.00 \\ 1.70 {\pm} 0.07 \\ 3.20 {\pm} 0.08 \end{array}$	$\begin{array}{c} 0.69{\pm}0.02\\ 0.79{\pm}0.00\\ 1.00{\pm}0.02\\ 1.48{\pm}0.02 \end{array}$	$0.96 \pm 0.04$ $1.18 \pm 0.01$ $1.56 \pm 0.03$ $2.82 \pm 0.20$	$0.79 \pm 0.02$ $0.87 \pm 0.01$ $1.01 \pm 0.00$ $1.38 \pm 0.07$	$\begin{array}{c} 0.86{\pm}0.05\\ 1.14{\pm}0.04\\ 1.55{\pm}0.02\\ \underline{2.48{\pm}0.22}\end{array}$	$0.75 \pm 0.02$ $0.85 \pm 0.01$ $0.99 \pm 0.01$ $1.30 \pm 0.06$	$0.92 \pm 0.19$ $1.18 \pm 0.02$ $1.61 \pm 0.09$ $2.91 \pm 0.04$	$\begin{array}{c} 0.76{\pm}0.08\\ 0.85{\pm}0.01\\ 1.00{\pm}0.04\\ 1.41{\pm}0.01\end{array}$	$\begin{array}{c} 0.94{\pm}0.06\\ 1.12{\pm}0.02\\ 1.47{\pm}0.11\\ 2.57{\pm}0.17\end{array}$	$\begin{array}{c} 0.77 {\pm} 0.03 \\ 0.86 {\pm} 0.01 \\ 0.97 {\pm} 0.03 \\ 1.31 {\pm} 0.07 \end{array}$	$\begin{array}{c} 0.96 {\pm} 0.04 \\ 1.11 {\pm} 0.01 \\ 1.60 {\pm} 0.04 \\ 2.85 {\pm} 0.16 \end{array}$	$\begin{array}{c} 0.78 {\pm} 0.01 \\ 0.84 {\pm} 0.00 \\ 1.01 {\pm} 0.02 \\ 1.39 {\pm} 0.04 \end{array}$	$\begin{array}{c} \underline{0.29 \pm 0.01} \\ \underline{0.63 \pm 0.05} \\ \underline{1.01 \pm 0.13} \\ \hline \textbf{1.41 \pm 0.24} \end{array}$	$\begin{array}{c} \underline{0.40 \pm 0.00} \\ 0.62 \pm 0.03 \\ \hline 0.81 \pm 0.05 \\ \hline 0.93 \pm 0.08 \end{array}$	$\begin{array}{c} 0.81{\pm}0.02\\ 1.13{\pm}0.05\\ 1.44{\pm}0.02\\ 2.06{\pm}0.16\end{array}$	$\begin{array}{c} 0.71 {\pm} 0.01 \\ 0.82 {\pm} 0.01 \\ 0.94 {\pm} 0.01 \\ 1.15 {\pm} 0.05 \end{array}$	0.27±0.00 0.61±0.04 0.94±0.12 1.77±0.13	0.40±0.01 0.61±0.02 0.78±0.05 1.05±0.07

• STAug stays the most robust with respect to original sample size



• STAug forecasts values that better align with the original time series



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## Conclusion

- Diverse and coherent augmentation for time-series forecasting
  - In the frequency domain, the re-combined subcomponents of original time series are both diverse and preserve the original basic components
  - In the time domain, we adapt "mix up" to generate diverse and in-between coherent samples by linearly interpolating past and future parts of series
- Experiments on five datasets show that STAug best reduces the forecasting errors of the base model compared with existing augmentation methods.

# Thanks!

Q&A